

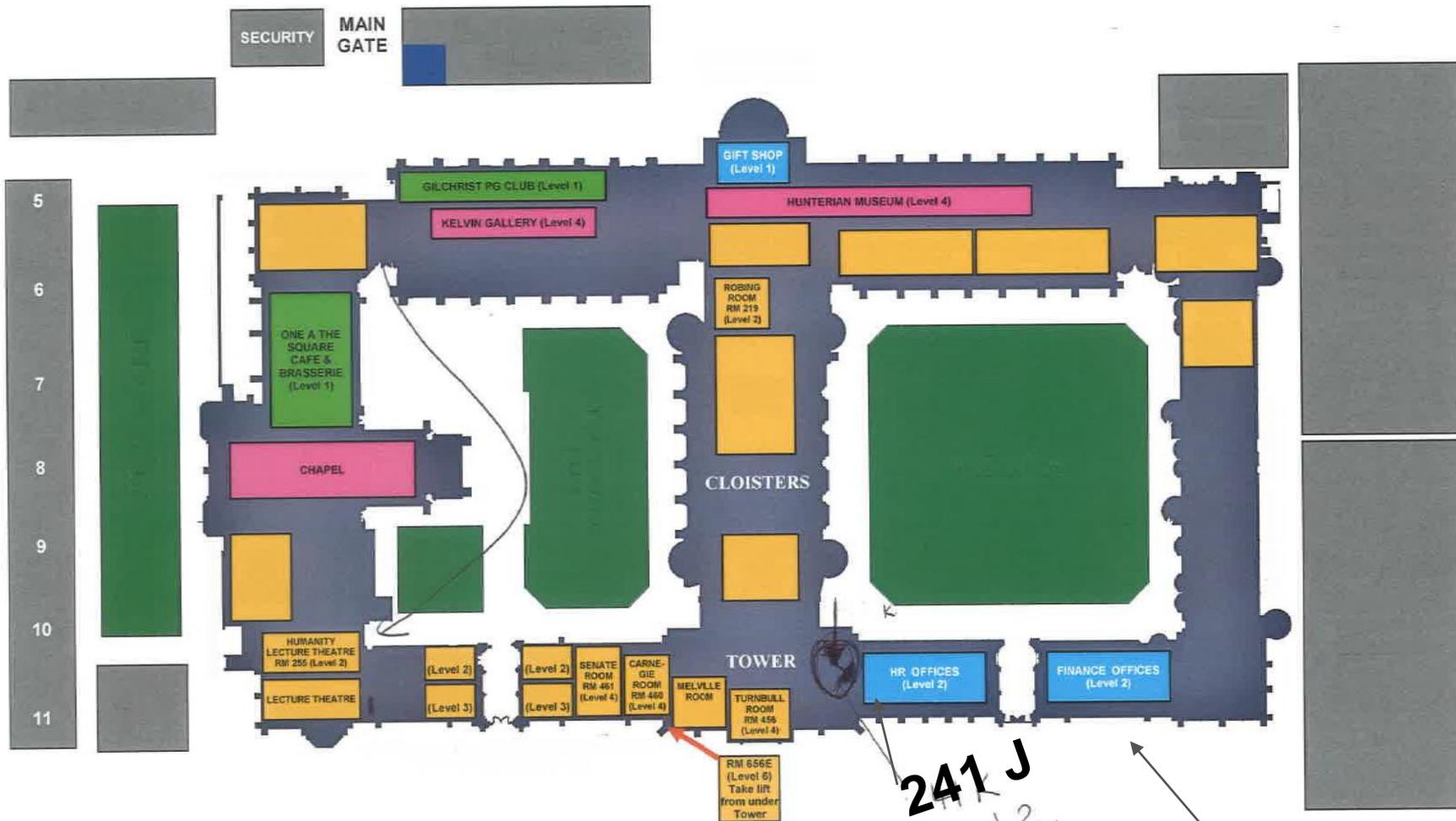
# **ECON 2A: Level 2 Microeconomics**

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Micro cluster

# Uncertainty

(Reading: Varian Chapter 12)

**Can you think of some examples :**

- **what is uncertain in economic systems?**
- **what are rational responses to uncertainty?**

## What is uncertain in economic systems?

- tomorrow's prices
- future wealth
- future availability of commodities
- present and future actions of other people
- .....

## What are rational responses to uncertainty?

- buying insurance (health, life, auto)
- a portfolio of contingent consumption goods - diversification
- Increasing the probability of the positive outcome (if you can)
- .....

# Diversification

- ◆ You have £100 to invest.
- ◆ Two firms, A and B. Shares of both firms cost £10 each
- ◆ With probability  $\frac{1}{2}$ ,
  - A' s profit is £100
  - B' s profit is £20.
- ◆ With probability  $\frac{1}{2}$ 
  - A' s profit is £20
  - B' s profit is £100.

**(A) If you buy only firm A' s stock**

$\text{£}100/10 = 10$  shares of A.

Expected earning:  $0.5 * \text{£}100 * 10 + 0.5 * \text{£}20 * 10 = \text{£}600$

**(B) If you buy only firm B' s stock**

$\text{£}100/10 = 10$  shares.

Expected earning:  $0.5 * \text{£}20 * 10 + 0.5 * \text{£}100 * 10 = \text{£}600$

## (C) If you buy 5 shares in each firm

Expected earning

$$= 0.5*(100*5 + 20*5) + 0.5*(20*5 + 100*5) = 600$$

Notice that you **earn £600 for sure**, irrespective of the state

- **diversification has reduced the risk.**

(But bear in mind that unlike this example, typically, diversification lowers risk in exchange for lowered expected earnings).

# Preference and Utility functions under Uncertainty

Think of a lottery:

- ◆ Outcome of the monetary winnings are:
  - win £90 with probability 1/2
  - £0 with probability 1/2.

Therefore the **Expected money value (EM)** of the lottery:

$$EM = \frac{1}{2} \times £90 + \frac{1}{2} \times £0 = 45$$

◆ Let Utility of the outcomes be:  $U(\pounds90) = 12$ ,  $U(\pounds0) = 2$ .

So, **Expected Utility (EU)**:

$$EU = \frac{1}{2} \times U(\pounds90) + \frac{1}{2} \times U(\pounds0)$$

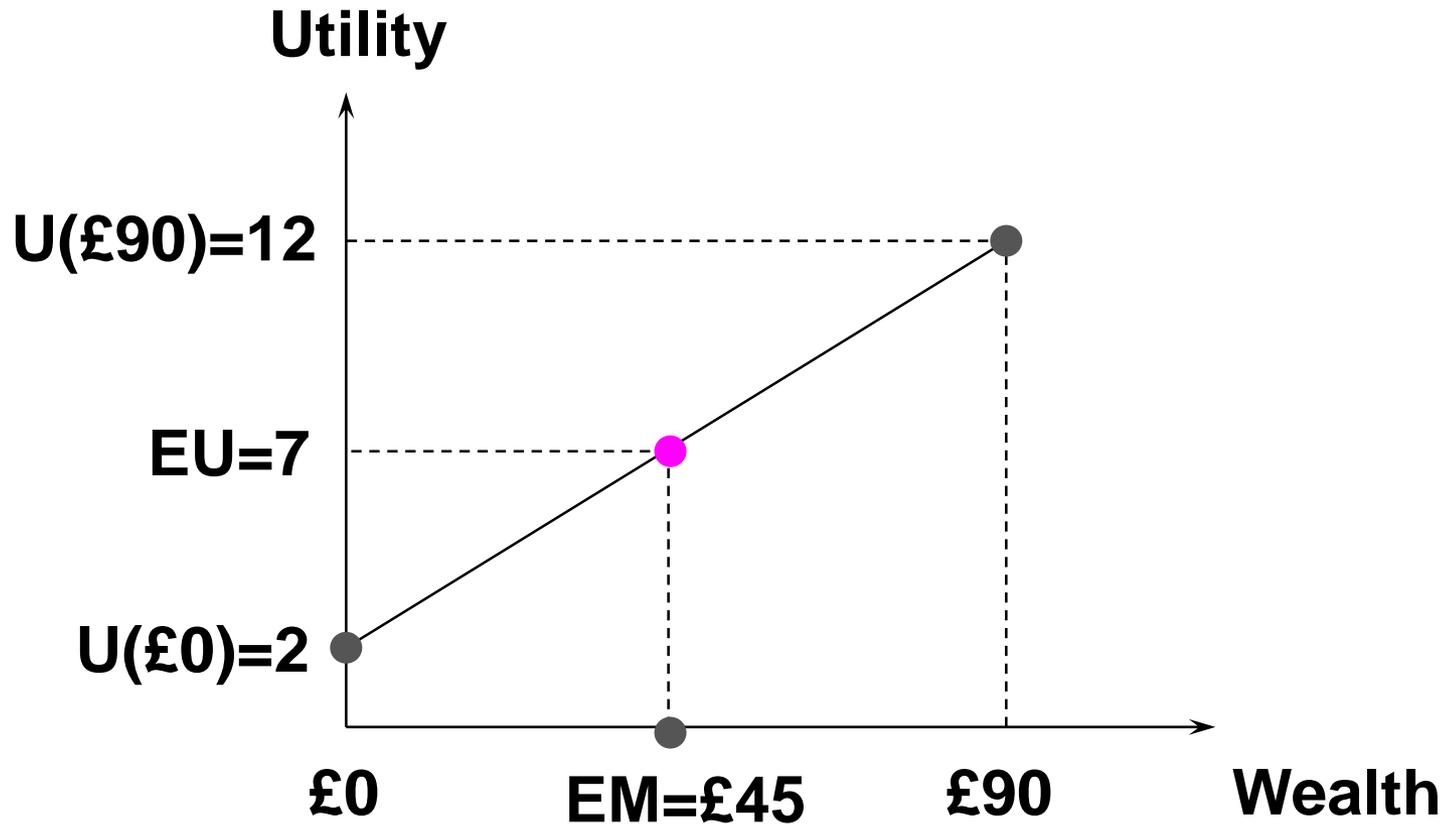
$$\begin{aligned} EU &= \frac{1}{2} \times 12 + \frac{1}{2} \times 2 \\ &= 6 + 1 = 7 \end{aligned}$$

What will be the EU if probability of winning is 75%?

(Each person's risk preference is different.)

$$EU = \frac{1}{2} \times U(\pounds 90) + \frac{1}{2} \times U(\pounds 0) = 7$$

$$EM = \frac{1}{2} \times \pounds 90 + \frac{1}{2} \times \pounds 0 = 45$$

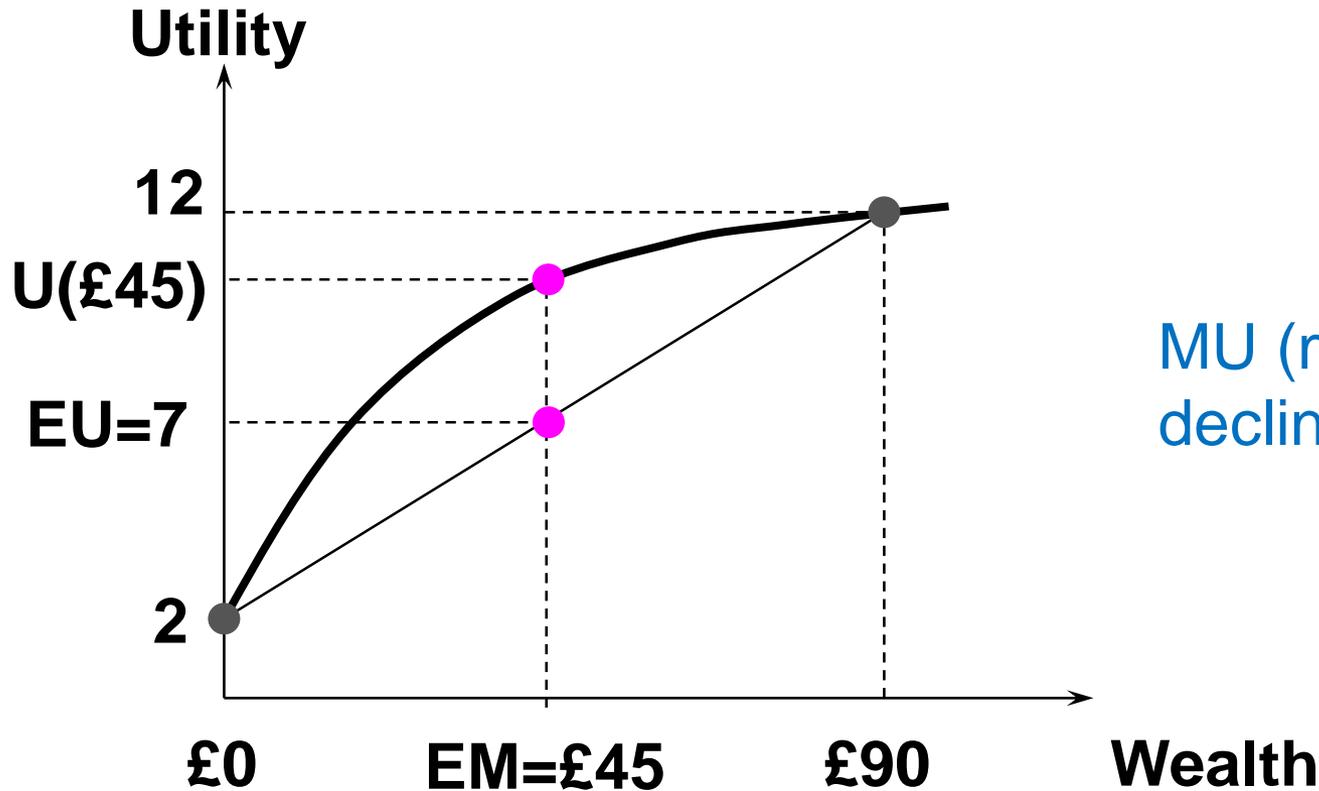


## Risk Averse:

If  $U(\pounds 45) > 7$ , receiving  $\pounds 45$  for sure is preferred to the lottery

$$U(\pounds 45) > EU \Rightarrow \text{risk-aversion.}$$

$$U(EM) > EU \Rightarrow \text{risk-aversion.}$$



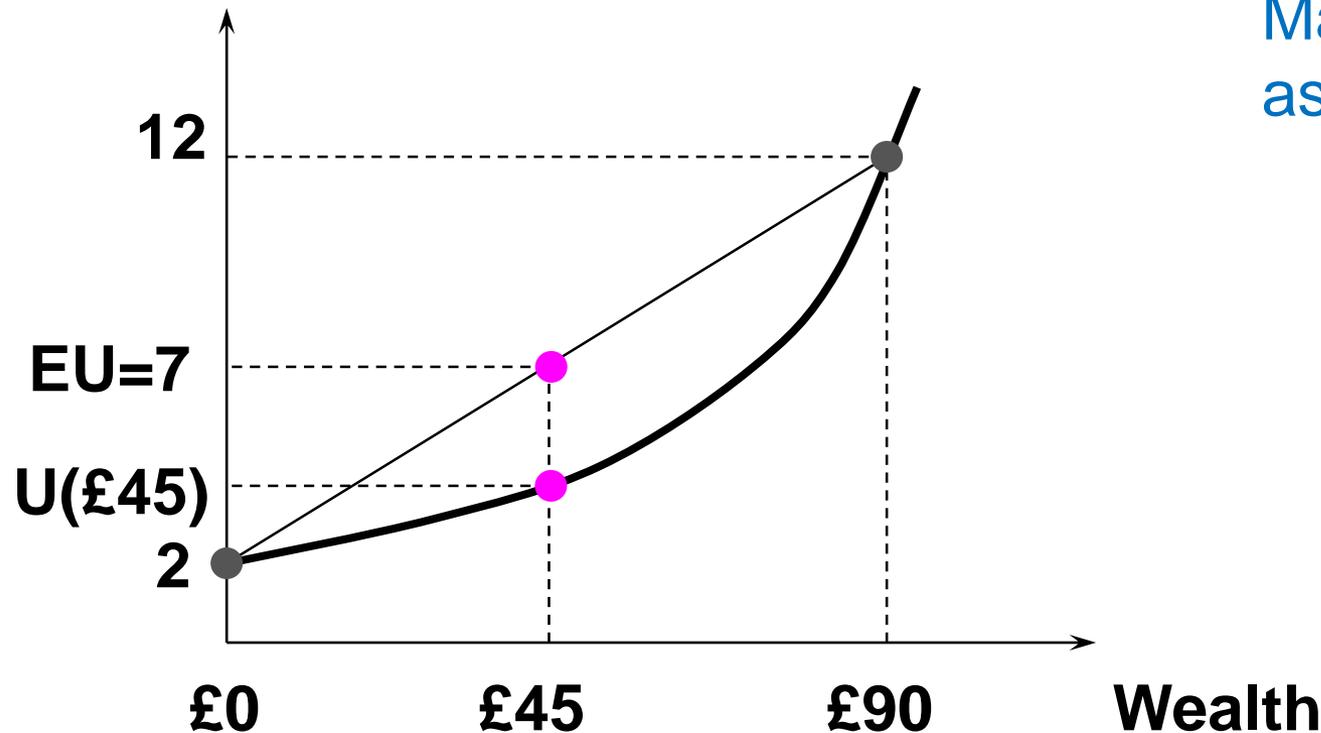
MU (marginal utility)  
declines as wealth rises.

# Risk-loving

If  $U(\pounds45) < 7$ , the lottery is preferred to receiving  $\pounds45$  for sure

$U(\pounds45) < EU \Rightarrow$  risk-loving.

$U(EM) < EU \Rightarrow$  risk-loving.



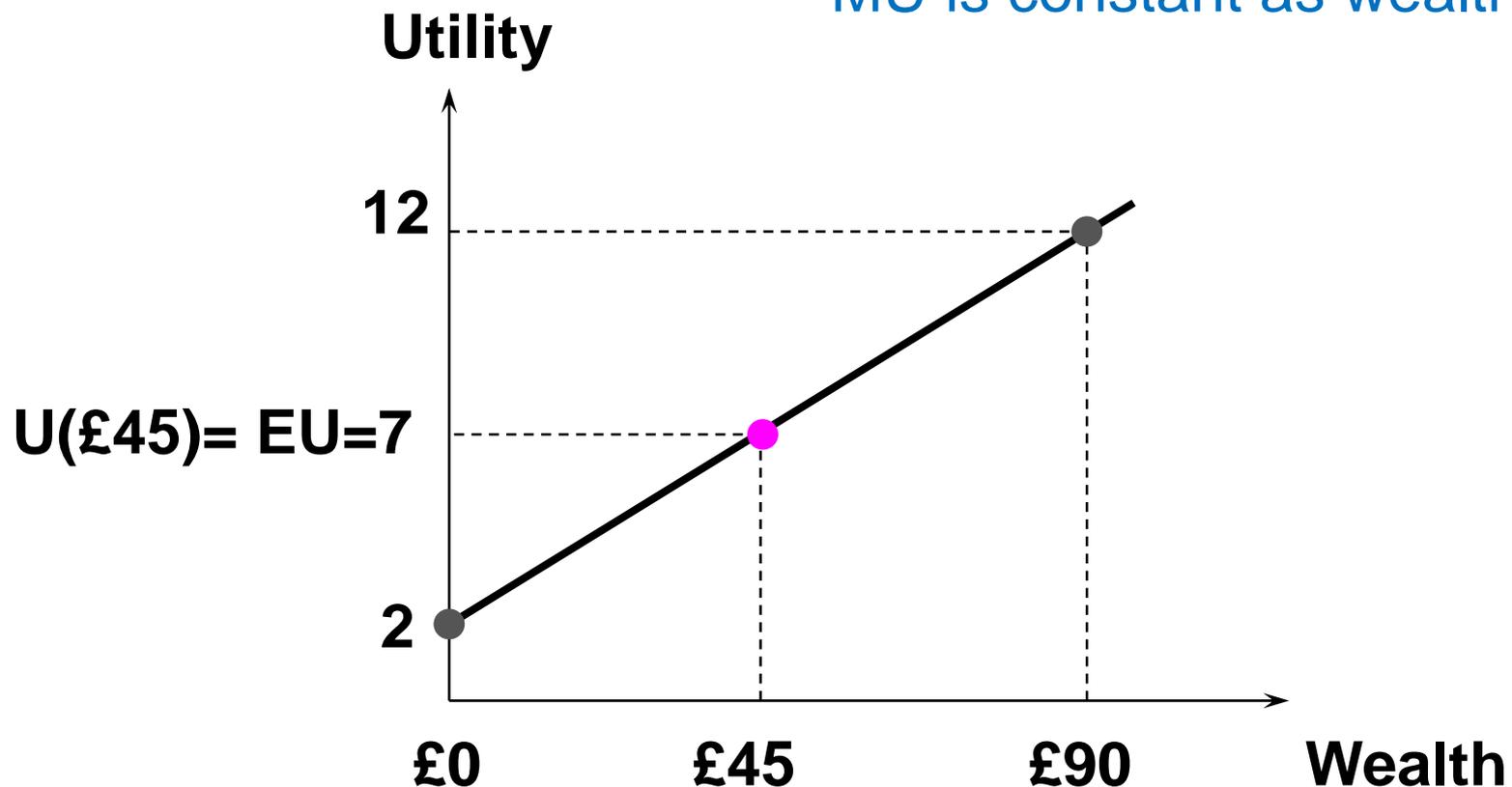
Marginal utility rises  
as wealth rises.

## Risk-neutral

If  $U(\pounds45) = 7$ , there is indifference between receiving  $\pounds45$  for sure and lottery.

$U(\pounds45) = EU \Rightarrow$  risk-neutrality.

MU is constant as wealth rises.



## Von Neumann-Morgenstern utility function

This is an expected utility function under uncertainty – when playing a lottery.

Geetha is thinking of betting on Roger Federer winning the ATP World Tour Finals.

She thinks the probability that he will not win is  $\pi_1$

and will win is  $\pi_2$ .

If she does not bet, she is **certain** to retain what she would have spent on betting.

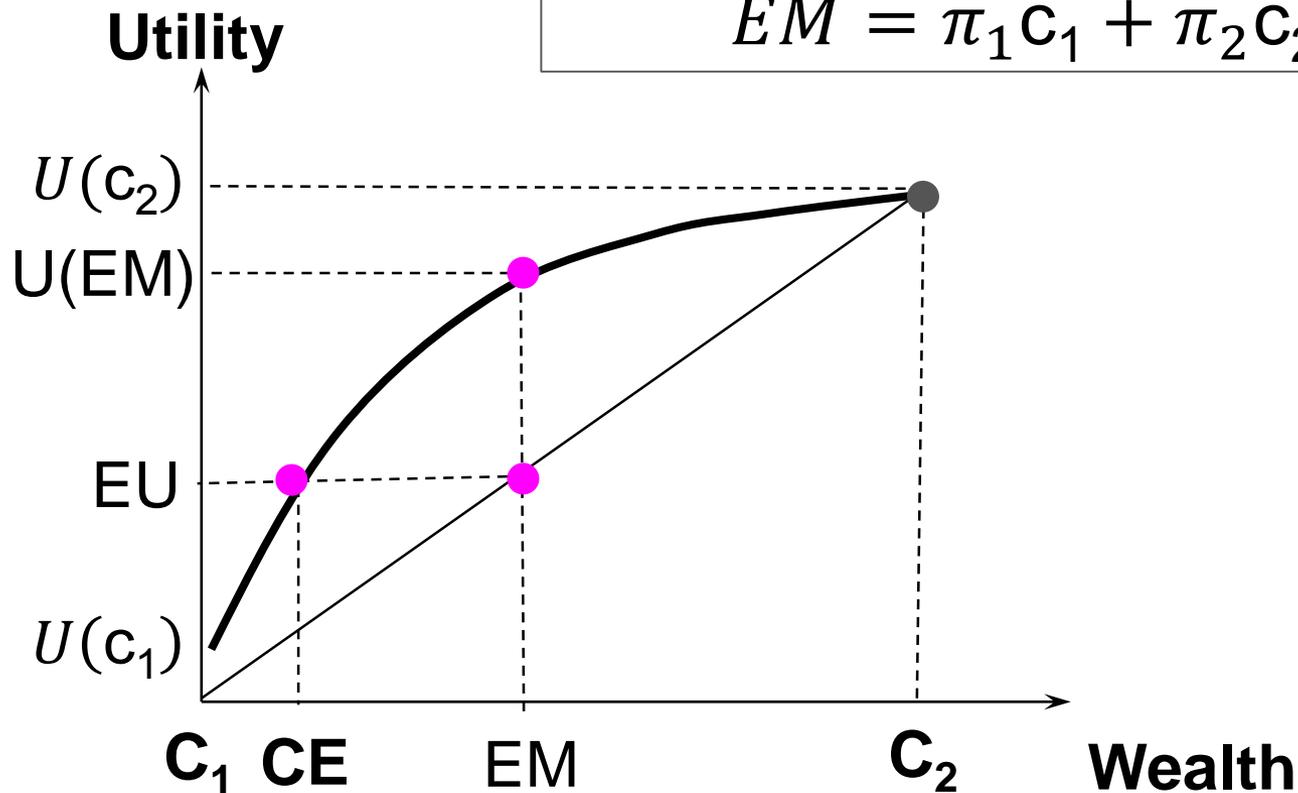
She gains  $c_2$  if she wins the bet, and  $c_1$  if she loses.

# Expected utility function

(or the von-Neumann-Morgenstern utility function):

$$EU = \pi_1 U(c_1) + \pi_2 U(c_2)$$

$$EM = \pi_1 c_1 + \pi_2 c_2$$



**Certainty Equivalent** (CE) is the value which will give the same utility as the expected utility.

$$U(CE) = EU$$

$$U(CE) = \pi_1 U(c_1) + \pi_2 U(c_2)$$

(If you know the functional form of  $U(\cdot)$ , you can solve for CE).

